

S. S Jain Subodh P.G. (Autonomous) College SUBJECT - Artificial Intelligence TITLE – The A* Algorithms

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The A* Algorithm



The Search Problem

Starting from a node n find the shortest path to a goal node g





Shortest Path

Consider the following weighted undirected graph:



We want: A path $5 \rightarrow v1 \rightarrow v2 \rightarrow ... \rightarrow 20$

Such that $g(20) = cost(5 \rightarrow v1) + cost(v1 \rightarrow v2) + ... + cost(\rightarrow 20)$ is minimum



Djikstra Algorithm

Greedy algorithm: from the candidate nodes select the one that has a path with minimum cost from the starting node





Djikstra Algorithm

Given a Graph G = (V,E) and T a subset of V, the fringe of T, is defined as:

 $Fringe(T) = \{ (w,x) \text{ in } E : w \in T \text{ and } x \in V - T \}$



Djikstra's algorithm pick the edge v in Fringe(T) that has minimum distance to the starting node \bigcirc g(v) is minimum



Example





Properties

Dijkstra's is a greedy algorithm

Why Dijkstra's Algorithm works?

The path from u to every node in T is the minimum path





Example



What does Djikstra's algorithm will do? (minimizing g(n)) **Problem**: Visit too many nodes, some *clearly* out of the question



Complexity

- Actual complexity is $O(|E|\log_2 |E|)$
- Is this good?

Actually it is bad for very large graphs!



Another Example: think of the search space in chess



Better Solution: Make a 'hunch"!

- Use *heuristics* to guide the search
 - Heuristic: estimation or "hunch" of how to search for a solution
- We define a heuristic function:

h(n) = "estimate of the cost of the cheapest path from the starting node to the goal node"





Lets Try A Heuristic



Heuristic: minimize h(n) = "Euclidean distance to destination"
Problem: not optimal (through Rimmici Viicea and Pitesti is shorter)



The A* Search

- **Difficulty**: we want to still be able to generate the path with minimum cost
- A* is an algorithm that:
 - Uses heuristic to guide search
 - While ensuring that it will compute a path with minimum cost

• "estimated cost"

• A* computes the function f(n) = g(n) + h(n)

"actual cost"



A*

- f(n) = g(n) + h(n)
 - g(n) = "cost from the starting node to reach n"
 - h(n) = "estimate of the cost of the cheapest path from n to the goal node"





Example



A*: minimize f(n) = g(n) + h(n)



Properties of A*

- A* generates an optimal solution if h(n) is an admissible heuristic and the search space is a tree:
 - h(n) is admissible if it never overestimates the cost to reach the destination node
- A* generates an optimal solution if h(n) is a consistent heuristic and the search space is a graph:
 - h(n) is consistent if for every node n and for every successor node n' of n:
 h(n) ≤ c(n,n') + h(n')



- If h(n) is consistent then h(n) is admissible
- •Frequently when h(n) is admissible, it is also consistent



Admissible Heuristics

- A heuristic is admissible if it is too optimistic, estimating the cost to be smaller than it actually is.
- Example:

In the road map domain,

h(n) = "Euclidean distance to destination"

is admissible as normally cities are not connected by roads that make straight lines



How to Create Admissible Heuristics

- Relax the conditions of the problem
 - This will result in admissible heuristics!
- 8-puzzle game:

• Possible heuristics?



Example: Admissible Heuristics in 8-Puzzle Game

- Heuristic: a tile A can be moved to any tile B
 - H1(n) = "number of misplaced tiles in board n"
- Heuristic: a tile A can be moved to a tile B if B is adjacent to A
 - H2(n) = "sum of distances of misplaced tiles to goal positions in board n"
- Some experimental results reported in Russell & Norvig (2002):
 - A* with h2 performs up to 10 times better than A* with h1
 - A* with h2 performs up to 36,000 times better than a classical uninformed search algorithm (iterative deepening)



h(n) = "# of goals remaining to be satisfied" <math>g(n) = "# of steps so far"



A* in Games

- Path finding (duh!)
 - We will have several presentations on the topic
 - We will see that sometimes even A* speed improvements are not sufficient
 - Additional improvements are required
- A* can be used for planning moves computer-controlled player (e.g., chess)
- F.E.A.R. uses A* to plan its search